



**Viernes, 27 de octubre de 2017.**

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## Number Theory meets Approximation Theory

### Abstract:

It is known that most real numbers are irrational and even transcendental, but if one singles out a particular real number, then it is not easy to show that it is irrational or transcendental. Usually this is done with a proof by contradiction, but there is a constructive way that uses approximation theory. Most of the famous mathematical constants, such as  $e$  and  $\pi$ , can be shown to be irrational by approximating them by rational numbers, but in such a way that the approximation is better than what would be possible for a rational number. The approximation can be polynomial approximation but most often it is rational approximation. Historically this was done using continued fractions, but Hermite proved the transcendence of  $e$  using Hermite-Padé approximants. I will give some more examples of this approach, in particular the zeta function evaluated at odd integers and its  $q$ -analog. The method also gives upper bounds for the measure of approximation.



Univ. Carlos III de Madrid



Coordenadas

**Hora** 11:00 - 12:00  
**Lugar** Seminario del Departamento de Matemáticas  
2.2 D08 Edificio Sabatini.

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